

Support Vector Machines

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Support Vector Machines

A different take on classification/regression

- Classification: Vapnick et al. (1963, 1992)
- Regression: Smola and Schölkopf (1998)

- Linear models
- But: can have non-linear transformations (and we can do these very efficiently)
- We don't explicitly represent the model parameters. Instead, the function is captured using a subset of the training samples

Support Vector Machines

Classification problem:

- Given: positive and negative samples (training set)
- Want to find a hyperplane that divides the set of points as “best” as possible
- Here: **best** means that we want to place the hyperplane so that it separates the points while being as far away from the points as possible

Quadratic Programming

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Quadratic Programming

Standard class of problems and corresponding algorithm:

- Minimize an objective function (quadratic, linear or mixture)
- Subject to a set of inequalities (\geq)

- Algorithm engages in a search:
 - Which equalities to satisfy ($=$) and which to allow to be unequal ($>$)
 - Values for each of the parameters

Quadratic Programming

- QP solvers are available in just about any serious mathematical tool kit, including numpy
- To use, one needs to transform your problem into a standard form

Soft-Boundary Classification

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Soft-Boundary Classification

- Many classification problems do not have a perfect linear solution
- We would like to explicitly acknowledge this, but still have a sense of maximum margin

Soft-Boundary Classification

Approach:

- Allow the algorithm to choose which samples to not have on the correct side of the margin
- Now have two objectives:
 - Minimize squared weights (which maximizes the boundary)
 - Minimize the misclassification error
 - Hyper-parameter: what is the balance between the two?

Non-Linear Preprocessing for SVMs

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Non-Linear Preprocessing for SVMs

- Support Vector Machines are inherently linear methods
- As with our earlier linear regression methods, we can apply non-linear transformations to the input features
- This gives us an effective way of expressing curved decision boundaries in the original feature space

Non-Linear Preprocessing for SVMs

If we choose our non-linear transformations carefully:

- Can create very large dimensional feature sets, which gives us the ability to be very expressive about decision boundaries
- Can also be computed very efficiently!

Kernel Functions

- We can use a $K()$ without having to explicitly articulate what the corresponding $\Phi()$
 - For the Gaussian kernel: $\Phi()$ is an infinite dimensional vector
- If we have two existing kernel functions ($K_1()$ and $K_2()$), then we can create new kernel functions:
 - $K_1() + K_2()$
 - $K_1() \times K_2()$

Kernel Function Implications

- Allow us to express a decision surface in a high-dimensional space without explicitly touching that space
 - Don't have to represent the feature vectors
 - Don't have to represent W
- For a single query, we have to touch all of the support vectors in the training set
 - The alphas are zero for the non-support vectors, so we can leave them out of the sum
 - The set of non-zero alphas can still be very large (an issue with large training sets)

Example: SVMs for Classification

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Example: SVMs for Classification

Scikit-learn provides several implementations of SVMs

- Some variation in parameters and naming
- Our focus: SVC
 - Based on the libsvm implementation

- Live demo

Support Vector Regression

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Support Vector Regression

- Basis: linear model
- Cost function: trade-off between explaining the training data and making the coefficients small
- Can transform into a dual problem where:
 - Queries are addressed using a weighted sum over the training set
 - The same ***kernel trick*** can be used to transform high-dimensional problem into a low-dimensional one

Example: Support Vector Regression

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Example: Support Vector Regression

Scikit-learn:

- LinearSVR
- SVR